

DEPARTMENT OF MATHEMATICS CHAPTER2-INVERSE TRIGONOMETRY

CLASS12

ONE MARK QUESTIONS

1. Write the principal value of

(i)
$$\sin^{-1}\left(-\frac{\sqrt{3}}{2}\right)$$

(ii)
$$\cos^{-1}(\sqrt{3}/2)$$

(iii)
$$\tan^{-1}\left(-\frac{1}{\sqrt{3}}\right)$$

(v)
$$\cot^{-1}\left(\frac{1}{\sqrt{3}}\right)$$

2. What is the value of the following functions (using principal value)

(i)
$$\tan^{-1}\left(\frac{1}{\sqrt{3}}\right) - \sec^{-1}\left(\frac{2}{\sqrt{3}}\right)$$

(i)
$$\tan^{-1}\left(\frac{1}{\sqrt{3}}\right) - \sec^{-1}\left(\frac{2}{\sqrt{3}}\right)$$
 (ii) $\sin^{-1}\left(-\frac{1}{2}\right) - \cos^{-1}\left(\frac{\sqrt{3}}{2}\right)$

(iii)
$$\tan^{-1}(1) - \cot^{-1}(-1)$$
 (iv) $\csc^{-1}(\sqrt{2}) + \sec^{-1}(\sqrt{2})$

(v)
$$\tan^{-1}(1) + \cot^{-1}(1) + \sin^{-1}(1)$$
.(vi) $\sin^{-1}\left(\sin\frac{4\pi}{5}\right)$

$$\sin^{-1}\left(\sin\frac{4\pi}{5}\right)$$

(vii)
$$tan^{-1}\left(tan\frac{5\pi}{6}\right)$$

(vii)
$$\tan^{-1}\left(\tan\frac{5\pi}{6}\right)$$
 (viii) $\csc^{-1}\left(\csc\frac{3\pi}{4}\right)$

3. If $tan^{-1} x + tan^{-1} y = \frac{4\pi}{5}$, find $cot^{-1} x + cot^{-1} y$.

4. Find the values of the following

$$\begin{array}{ll} \text{(i)} & \sin\left\{\frac{\pi}{6}-\sin^{-1}\!\left(-\frac{\sqrt{3}}{2}\right)\right\} & \text{(ii)} & \tan^{-1}\left(\sin\!\left(-\frac{\pi}{2}\right)\right) \\ \text{(iii)} & \tan\left(\cos^{-1}\frac{8}{17}\right) & \text{(iv)} & \sin^{-1}\left(\cos\!\left(\sin^{-1}\frac{\sqrt{3}}{2}\right)\right) \end{array}$$

(ii)
$$tan^{-1} \left(sin \left(-\frac{\pi}{2} \right) \right)$$

(iii)
$$\tan \left(\cos^{-1}\frac{8}{17}\right)$$

(iv)
$$\sin^{-1}\left(\cos\left(\sin^{-1}\frac{\sqrt{3}}{2}\right)\right)$$

5. Evaluate the following

(i)
$$\sin (2 \sin^{-1} (0.6))$$

(iii)
$$\sin\left(2\cos^{-1}\left(-\frac{5}{15}\right)\right)$$

(iii)
$$\sin\left(2\cos^{-1}\left(-\frac{5}{15}\right)\right)$$
 (iv) $\tan\left(\frac{1}{2}\cos^{-1}\left(\frac{\sqrt{5}}{3}\right)\right)$

6. If $\tan^{-1}x + \tan^{-1}y = \frac{\pi}{4}$, xy < 1, then the value of x + y + xy. 7. If $3 \tan^{-1}x + \cot^{-1}x = \pi$, then find the value of x.

8. If
$$\cos\left(\sin^{-1}\frac{2}{5}+\cos^{-1}x\right)=0$$
, then find the value of x.

9. If $\sin^{-1}x + \sin^{-1}y = \frac{\pi}{2}$, then find the value of $\cos^{-1}x + \cos^{-1}y$.

10. If $\cos^{-1}\alpha + \cos^{-1}\beta + \cos^{-1}\gamma = 3\pi$, then find the value of $\alpha(\alpha + \gamma) + \beta(\alpha + \gamma) + \gamma(\alpha + \beta)$.

11. If $\tan^{-1}x - \cot^{-1}x = \tan^{-1}\left(\frac{1}{\sqrt{3}}\right)$, the find the value of x:

12. Find the value of tan2 (sec-12) + cot2 (cosec-13)

Evaluate sin {cot⁻¹(cos (tan⁻¹1))}

14. If $a \le 2 \sin^{-1}x + \cos^{-1}x \le b$, then find the value of a and b.

15. Solve
$$\cos^{-1}(\sin(\cos^{-1}x)) = \frac{\pi}{3}$$

16. Write the value of
$$\tan \left(2\tan^{-1}\frac{1}{5}\right)$$

17. Write the value of
$$Sec^{-1}\left(sec\left(-\frac{8\pi}{5}\right)\right)$$

TWO MARK QUESTIONS

1. Find the value of the following

(i)
$$\sin^{-1}\left(-\frac{\sqrt{3}}{2}\right) + \cos^{-1}\left(-\frac{1}{2}\right) + \tan^{-1}\left(-\frac{1}{\sqrt{3}}\right)$$

(ii)
$$\sin^{-1}\left(\sin\frac{2\pi}{3}\right) + \cos^{-1}\left(\cos\frac{4\pi}{3}\right)$$

(iii)
$$\sin \left\{ \frac{\pi}{3} - \sin^{-1} \left(-\frac{1}{2} \right) \right\}$$

(iv)
$$\tan^{-1}\left(\tan\frac{7\pi}{6}\right)$$
: $\cos^{-1}\left(\cos\frac{7\pi}{6}\right)$

Simplify

(i)
$$\tan^{-1}\left(\frac{\sin x}{1+\cos x}\right)$$

(ii)
$$\cot^{-1}\left(\frac{1}{\sqrt{x^2-1}}\right), x < -1$$

(iii)
$$\cos \left\{ \cos^{-1} \left(\frac{-\sqrt{3}}{2} \right) + \frac{\pi}{6} \right\}$$

(iv)
$$\tan \left[\frac{1}{2}\cos^{-1}\left(\frac{3}{\sqrt{11}}\right)\right]$$

3. Simplify: $\sin^{-1} \left\{ \frac{\sin x + \cos x}{\sqrt{2}} \right\}, -\frac{\pi}{4} < x < \frac{\pi}{4}$

4 MARK QUESTIONS

1. Show that : $\tan^{-1} \left[\frac{\sqrt{1 + \cos x} + \sqrt{1 - \cos x}}{\sqrt{1 + \cos} - \sqrt{1 - \cos x}} \right] = \frac{\pi}{4} + \frac{x}{2}; x \in [0, \pi]$

2.

Prove that:

$$\tan^{-1}\left(\frac{\sqrt{1+x^2}+\sqrt{1-x^2}}{\sqrt{1+x^2}-\sqrt{1-x^2}}\right) = \frac{\pi}{4} + \frac{1}{2}\cos^{-1}x^2$$

3.

Prove that:

$$\tan\left[\frac{\pi}{4} + \frac{1}{2}tan^{-1}\left(\frac{a}{b}\right)\right] + \tan\left[\frac{\pi}{4} - \frac{1}{2}tan^{-1}\left(\frac{a}{b}\right)\right] = \frac{2\sqrt{a^2 + b^2}}{b}$$

4.

Prove that $\tan \left(\frac{\pi}{4} + \frac{1}{2}\cos^{-1}\frac{a}{b}\right) + \tan\left(\frac{\pi}{4} - \frac{1}{2}\cos^{-1}\frac{a}{b}\right) = \frac{2b}{a}$

ANSWERS

ONE MARK QUESTIONS

1. (i)
$$-\frac{\pi}{3}$$
 (ii) $\frac{\pi}{6}$ (iii) $\frac{-\pi}{6}$ (iv) $\frac{-\pi}{6}$ (v) $\frac{\pi}{3}$ (vi) $\frac{2\pi}{3}$

$$(ii)\frac{\pi}{6}$$

(iii)
$$\frac{-\pi}{6}$$

(iv)
$$\frac{-\pi}{6}$$

$$(v)\frac{\pi}{2}$$

(vi)
$$\frac{2\pi}{2}$$

(ii)
$$\frac{-\pi}{3}$$

2. (i) 0 (ii)
$$\frac{-\pi}{3}$$
 (iii) $-\frac{\pi}{2}$ (iv) $\frac{\pi}{2}$

(v)
$$\pi$$
 (vi) $\frac{\pi}{5}$ (vii) $\frac{-\pi}{6}$ (Viii) $\frac{\pi}{4}$

(Viii)
$$\frac{\pi}{4}$$

(ii)
$$-\frac{\pi}{4}$$

(iii)
$$-\frac{15}{8}$$

(iv)
$$\frac{\pi}{6}$$

(iii)
$$-\frac{120}{169}$$

(i) 1 (ii)
$$-\frac{\pi}{4}$$
 (iii) $-\frac{15}{8}$ (iv) $\frac{\pi}{6}$ (i) 0.96 (ii) 0.96 (iii) $-\frac{120}{169}$ (iv) $\frac{3-\sqrt{5}}{2}$

8.
$$x = \frac{2}{5}$$

9.
$$\frac{\pi}{2}$$

11.
$$x = \sqrt{3}$$

13.
$$\sqrt{\frac{2}{3}}$$

14.
$$a = 0, b = \pi$$

10. 6
13.
$$\sqrt{\frac{2}{3}}$$

15. $x = \frac{\sqrt{3}}{2}$
17. $\frac{2\pi}{5}$

17.
$$\frac{2\pi}{5}$$

TWO MARK QUESTIONS

1. (i)
$$\frac{\pi}{6}$$

2. (i)
$$\frac{x}{2}$$

(ii)
$$\pi - \sec^{-1}$$

1. (i)
$$\frac{\pi}{6}$$
 (ii) π (iii) 1 (iv) π
2. (i) $\frac{x}{2}$ (ii) $\pi - \sec^{-1} x$ (iii) -1 (iv) $\frac{\sqrt{11} - 3}{\sqrt{2}}$

3.
$$x + \frac{\pi}{4}$$
 7. $\frac{\pi}{4}$

7.
$$\frac{\pi}{4}$$